



## Groomer's Challenge

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### Questions 1–6

Setup:

- three groomers: L M N
- 1-hour appointment slots: 8 9 10
- seven animals: P P P P T T W
- no more than one animal per appointment slot

Conditions:

#1: L  $\longrightarrow$  more animals than M and N

#2:  $\left. \begin{array}{l} T \\ P \end{array} \right\} 1^+$

#3: each groomer  $\longrightarrow 2^+$  types

#4:  $P_{N10}$

#5:  $\cancel{TP}$

#6:  $\sim P_M$  first

Overview:

Combining the first and third conditions, we can infer a respective allocation of animals to L, M, and N of 3, 2, 2. From the third condition, and the fact that there are four Ps, we can infer that L grooms two Ps and each of M and N grooms one P. Since L grooms two Ps, the second and fifth conditions dictate that she must groom the Ps at 8 AM and 10 AM. The fifth condition further dictates that both Ts must be groomed at 9 AM. Since M must groom a P, Ps cannot be groomed at 9 AM (fifth condition), and M cannot groom a P at 8 AM (sixth condition), M must groom a P at 10 AM. The only uncertainty remaining about L's schedule is whether she grooms a T or the W at 9 AM, and we can set up three molds to represent all the acceptable solutions.

<p>#1</p> <table style="width: 100%; border-collapse: collapse;"> <tr><td style="text-align: center;">10</td><td style="text-align: center;">P</td><td style="text-align: center;">P</td><td style="text-align: center;">P</td></tr> <tr><td style="text-align: center;">9</td><td style="text-align: center;">W</td><td style="text-align: center;">T</td><td style="text-align: center;">T</td></tr> <tr><td style="text-align: center;">8</td><td style="text-align: center;">P</td><td style="text-align: center;">X</td><td style="text-align: center;">X</td></tr> <tr><td></td><td style="text-align: center;">L</td><td style="text-align: center;">M</td><td style="text-align: center;">N</td></tr> </table>	10	P	P	P	9	W	T	T	8	P	X	X		L	M	N	<p>#2</p> <table style="width: 100%; border-collapse: collapse;"> <tr><td style="text-align: center;">10</td><td style="text-align: center;">P</td><td style="text-align: center;">P</td><td style="text-align: center;">P</td></tr> <tr><td style="text-align: center;">9</td><td style="text-align: center;">T</td><td style="text-align: center;">T</td><td style="text-align: center;">X W</td></tr> <tr><td style="text-align: center;">8</td><td style="text-align: center;">P</td><td style="text-align: center;">X</td><td style="text-align: center;">W X</td></tr> <tr><td></td><td style="text-align: center;">L</td><td style="text-align: center;">M</td><td style="text-align: center;">N</td></tr> </table>	10	P	P	P	9	T	T	X W	8	P	X	W X		L	M	N	<p>#3</p> <table style="width: 100%; border-collapse: collapse;"> <tr><td style="text-align: center;">10</td><td style="text-align: center;">P</td><td style="text-align: center;">P</td><td style="text-align: center;">P</td></tr> <tr><td style="text-align: center;">9</td><td style="text-align: center;">T</td><td style="text-align: center;">X W</td><td style="text-align: center;">T</td></tr> <tr><td style="text-align: center;">8</td><td style="text-align: center;">P</td><td style="text-align: center;">W X</td><td style="text-align: center;">X</td></tr> <tr><td></td><td style="text-align: center;">L</td><td style="text-align: center;">M</td><td style="text-align: center;">N</td></tr> </table>	10	P	P	P	9	T	X W	T	8	P	W X	X		L	M	N
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**Mold #1:** If L grooms the W, M and T must each groom a T at 9, and they must therefore not have appointments at 8.

**Mold #2:** If L grooms a T and M grooms a T, N will groom the W at either 8 or 9.

**Mold #3:** If L grooms a T and P grooms a T, M will groom the W at either 8 or 9.

1. (D) As we inferred, M must be assigned exactly two animals, and choice D is therefore correct.



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2. **(B)** Comparing the choices to our molds reveals that only B must be false.
3. **(A)** Plugging this information into our molds reveals that only choice A must be true.
4. **(E)** Mold #1 is the only one of the three with only one solution. We based it on L grooming the W, and choice E is therefore correct.
5. **(C)** This is true of both molds #1 and #2. Since M cannot groom both a T and the W, choice C must be false.
6. **(E)** This doesn't change the fact that N must groom a P. Since none of the Ps can be groomed at 9, N must groom a P at 8. Thus, L and M must each groom a T at 9. Only choice E is not compatible with this solution, and it must therefore be false.

10	<u>P</u>	<u>P</u>	<u>W</u>
9	<u>T</u>	<u>T</u>	<u>X</u>
8	<u>P</u> L	<u>X</u> M	<u>P</u> N